

Dark Matter Production During Reheating (*by example*)

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CONSEJO SUPERIOR DE INVESTIGACIONES CIENTÍFICAS

1. DM model



2. Reheating



3. Freeze-in



4. Constraints



Is a spin- $\frac{3}{2}$ dark matter particle the missing piece in the puzzle?

Described by Rarita-Schwinger Lagrangian

$$\mathcal{L}_{3/2}^0 = -\frac{1}{2} \bar{\Psi}_\mu (i\gamma^{\mu\rho\nu} \partial_\rho + m_{3/2} \gamma^{\mu\nu}) \Psi_\nu$$

with $\gamma^{\mu\nu} = \gamma^{[\mu} \gamma^{\nu]}$ and $\gamma^{\mu\nu\rho} = \gamma^{[\mu} \gamma^\nu \gamma^{\rho]}$.

1. DM model



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with $\gamma^{\mu\nu} = \gamma^{[\mu} \gamma^{\nu]}$ and $\gamma^{\mu\nu\rho} = \gamma^{[\mu} \gamma^\nu \gamma^{\rho]}$.

Instead of highly symmetric WIMP/gravitino-like scenario, consider a minimal embedding,

$$\begin{aligned} \mathcal{L} = & \mathcal{L}_{\text{SM}} + \mathcal{L}_{3/2}^0 + \mathcal{L}_{\nu_R}^0 + yH\bar{\nu}_L\nu_R + \frac{M_R}{2} \bar{\nu}_R^c \nu_R \\ & + i\frac{\alpha_1}{2M_P} \bar{\nu}_R \gamma^\mu [\gamma^\rho, \gamma^\sigma] \Psi_\mu F_{\rho\sigma} + i\frac{\alpha_2}{2M_P} i\sigma_2 (D^\mu H)^* \bar{L} \Psi_\mu + \text{h.c.} \end{aligned}$$

MG, Y. Mambrini, K. A. Olive and S. Verner, PRD 102 (2020), 083533

1. DM model



2. Reheating



3. Freeze-in

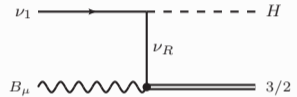
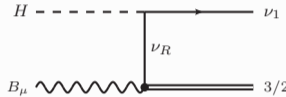
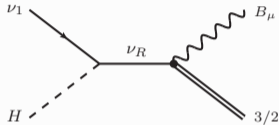


4. Constraints

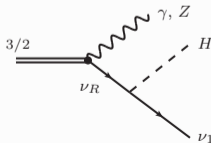
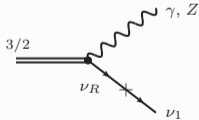


Scatterings and decays

$$\mathcal{L}_{3/2} = i \frac{\alpha_1}{2M_P} \bar{\nu}_R \gamma^\mu [\gamma^\rho, \gamma^\sigma] \Psi_\mu F_{\rho\sigma} + i \frac{\alpha_2}{2M_P} i\sigma_2 (D^\mu H)^* \bar{L} \Psi_\mu + \text{h.c.}$$



$$\sigma(s) = \frac{11\alpha_1^2 y^2 s^2}{72\pi m_{3/2}^2 M_R^2 M_P^2}, \quad s = E_{\text{CM}}^2$$



$$\tau_{3/2}^{2b} \simeq 1.6 \times 10^{29} \left(\frac{10^{-2}}{y\alpha_1} \right)^2 \left(\frac{M_R}{10^{14} \text{ GeV}} \right)^2 \left(\frac{10^4 \text{ GeV}}{m_{3/2}} \right)^3 \text{ s}$$

$$\tau_{3/2}^{3b} \simeq 5.6 \times 10^{28} \left(\frac{10^{-2}}{y\alpha_1} \right)^2 \left(\frac{M_R}{10^{14} \text{ GeV}} \right)^2 \left(\frac{10^4 \text{ GeV}}{m_{3/2}} \right)^5 \text{ s}$$

1. DM model



2. Reheating



3. Freeze-in

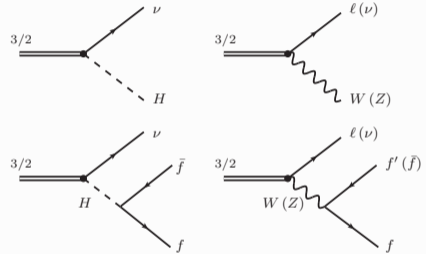
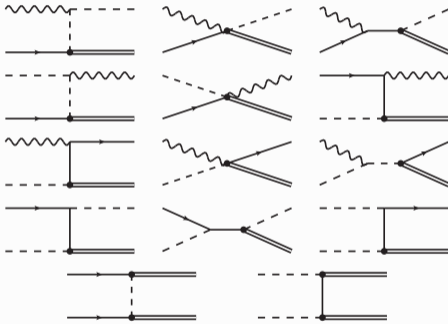


4. Constraints



Scatterings and decays

$$\mathcal{L}_{3/2} = i\frac{\alpha_1}{2M_P}\bar{\nu}_R\gamma^\mu[\gamma^\rho,\gamma^\sigma]\Psi_\mu F_{\rho\sigma} + \boxed{i\frac{\alpha_2}{2M_P}i\sigma_2(D^\mu H)^*\bar{L}\Psi_\mu} + \text{h.c.}$$



$$\sigma(s) = \frac{\alpha_2^2 s}{9216\pi m_{3/2}^2 M_P^2} (639g^2 + 87g'^2 + 144h_t^2 + 32h_\tau^2)$$

$$\frac{\tau_{3/2}}{10^{28}\text{s}} \simeq \begin{cases} 14.8 \left(\frac{10^{-7}}{\alpha_2}\right)^2 \left(\frac{1\text{ GeV}}{m_{3/2}}\right)^3, & m_{3/2} > m_H \\ 0.6 \left(\frac{10^{-3}}{\alpha_2}\right)^2 \left(\frac{1\text{ GeV}}{m_{3/2}}\right)^{5.28}, & m_e < m_{3/2} < m_W \\ 4.8 \left(\frac{10^{-3}}{\alpha_2}\right)^2 \left(\frac{1\text{ GeV}}{m_{3/2}}\right)^5, & m_{3/2} < m_e \end{cases}$$

1. DM model



2. Reheating



3. Freeze-in



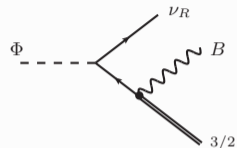
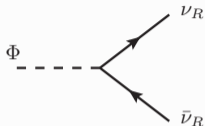
4. Constraints



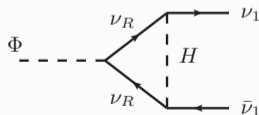
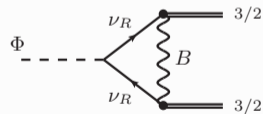
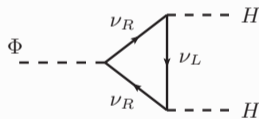
Production (via inflaton decay)

Assume $\mathcal{L}_\Phi \supset y_\nu \Phi \bar{\nu}_R \nu_R$. Via α_1 ,

$M_R \ll m_\Phi$:



$M_R \gg m_\Phi$:



(via α_2 are 2-loop suppressed)

1. DM model



2. Reheating



3. Freeze-in

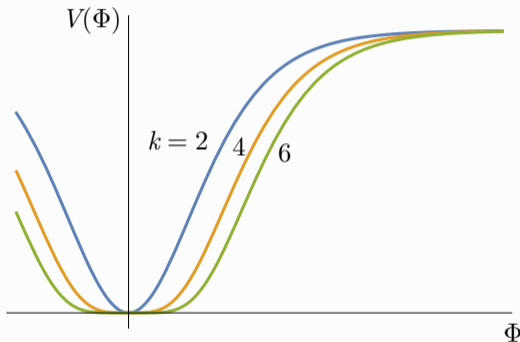


4. Constraints



Reheating

After inflation, the Universe is reheated through the decay of the inflaton Φ



$$V(\Phi) = \lambda M_P^4 \left[\sqrt{6} \tanh \left(\frac{\Phi}{\sqrt{6} M_P} \right) \right]^k \xrightarrow{\Phi \ll M_P} \lambda \frac{\Phi^k}{M_P^{k-4}}$$

R. Kallosh and A. Linde, JCAP 07 (2013), 002

$$\begin{aligned} \dot{\rho}_\Phi + 3H(\rho_\Phi + P_\Phi) &= 0 \\ 3H^2 M_P^2 &= \rho_\Phi \end{aligned}$$

where

$$\begin{aligned} \rho_\Phi &= \frac{1}{2} \dot{\Phi}^2 + V(\Phi) \\ P_\Phi &= \frac{1}{2} \dot{\Phi}^2 - V(\Phi) \end{aligned}$$

1. DM model



2. Reheating



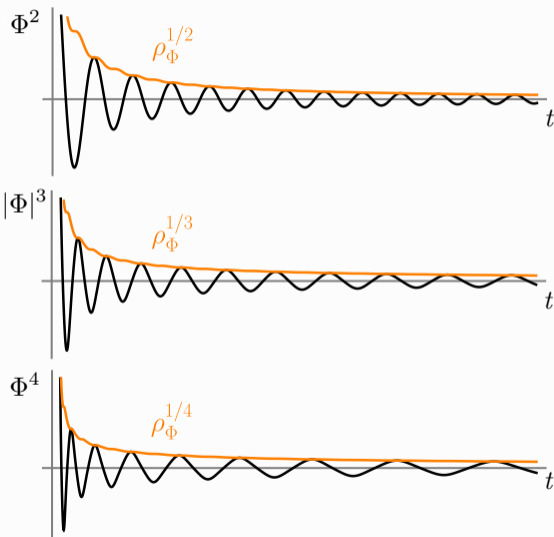
3. Freeze-in



4. Constraints



Inflaton oscillation



\sim matter

$$\rho_\Phi = \rho_{\text{end}} \left(\frac{a}{a_{\text{end}}} \right)^{-\frac{6k}{k+2}}$$
$$a \propto t^{\frac{k+2}{3k}}$$

\sim radiation

1. DM model



2. Reheating



3. Freeze-in



4. Constraints

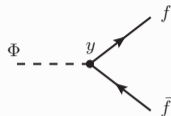


Decay of the inflaton

$$\dot{\rho}_{\Phi} + 3 \left(\frac{2k}{k+2} \right) H \rho_{\Phi} = -\Gamma_{\Phi}(t) \rho_{\Phi}$$

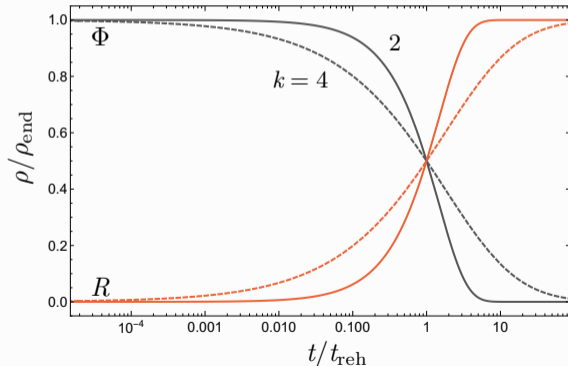
$$\dot{\rho}_R + 4H\rho_R = \Gamma_{\Phi}(t)\rho_{\Phi}$$

$$3M_P^2 H^2 = \rho_{\Phi} + \rho_R$$



$$\Gamma_{\Phi} = \frac{y^2}{8\pi} m_{\Phi}(t),$$

$$m_{\Phi}^2 \equiv \partial_{\Phi}^2 V(\Phi) \propto \rho_{\Phi}^{\frac{k-2}{k}}$$



1. DM model



2. Reheating



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4. Constraints



Decay of the inflaton

$$\dot{\rho}_\Phi + 3 \left(\frac{2k}{k+2} \right) H \rho_\Phi = -\Gamma_\Phi(t) \rho_\Phi$$

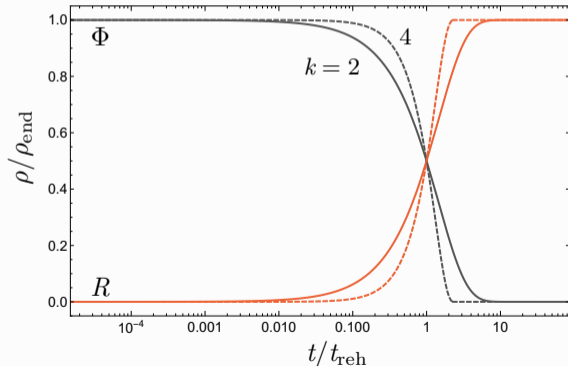
$$\dot{\rho}_R + 4H\rho_R = \Gamma_\Phi(t)\rho_\Phi$$

$$3M_P^2 H^2 = \rho_\Phi + \rho_R$$



$$\Gamma_\Phi = \frac{\mu^2}{8\pi m_\Phi(t)},$$

$$m_\Phi^2 \equiv \partial_\Phi^2 V(\Phi) \propto \rho_\Phi^{\frac{k-2}{k}}$$



1. DM model



2. Reheating



3. Freeze-in



4. Constraints

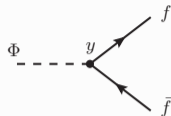


Decay of the inflaton

$$\dot{\rho}_{\Phi} + 3 \left(\frac{2k}{k+2} \right) H \rho_{\Phi} = -\Gamma_{\Phi}(t) \rho_{\Phi}$$

$$\dot{\rho}_R + 4H\rho_R = \Gamma_{\Phi}(t)\rho_{\Phi}$$

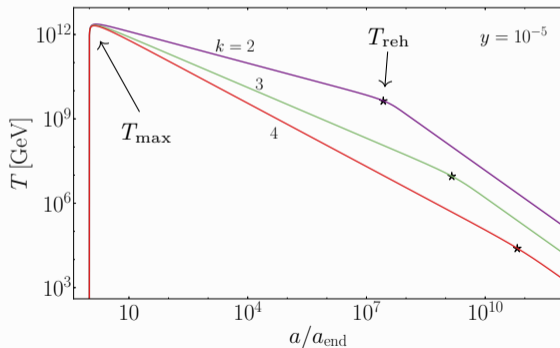
$$3M_P^2 H^2 = \rho_{\Phi} + \rho_R$$



$$\Gamma_{\Phi} = \frac{y^2}{8\pi} m_{\Phi}(t),$$

$$m_{\Phi}^2 \equiv \partial_{\Phi}^2 V(\Phi) \propto \rho_{\Phi}^{\frac{k-2}{k}}$$

$$T = \left(\frac{30\rho_R}{\pi^2 g_*} \right)^{1/4}$$
$$\propto a^{-\frac{3}{2} \frac{k-3}{k+4}}$$



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2. Reheating



3. Freeze-in



4. Constraints

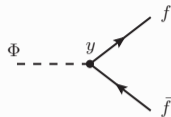


Decay of the inflaton

$$\dot{\rho}_\Phi + 3 \left(\frac{2k}{k+2} \right) H \rho_\Phi = -\Gamma_\Phi(t) \rho_\Phi$$

$$\dot{\rho}_R + 4H\rho_R = \Gamma_\Phi(t) \rho_\Phi$$

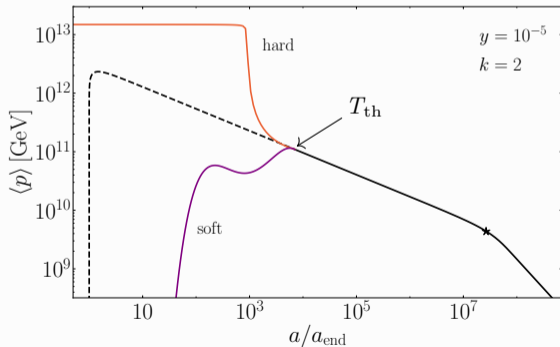
$$3M_P^2 H^2 = \rho_\Phi + \rho_R$$



$$\Gamma_\Phi = \frac{y^2}{8\pi} m_\Phi(t),$$

$$m_\Phi^2 \equiv \partial_\Phi^2 V(\Phi) \propto \rho_\Phi^{\frac{k-2}{k}}$$

$$\Gamma_\Phi t_{\text{th}} \simeq \alpha_{\text{SM}}^{-16/5} \left(\frac{\Gamma_\Phi m_\Phi^2}{M_P^3} \right)^{2/5}$$



1. DM model



2. Reheating



3. Freeze-in



4. Constraints



Freeze-in during reheating

For the out-of-equilibrium process $i + j + \dots \rightarrow \Psi + a + b + \dots$,

$$\begin{aligned} \frac{\partial f_{3/2}}{\partial t} - H|\mathbf{p}| \frac{\partial f_{3/2}}{\partial |\mathbf{p}|} &\simeq \frac{1}{2p_0} \int \frac{g_a d^3 \mathbf{p}_a}{(2\pi)^3 2p_{a0}} \frac{g_b d^3 \mathbf{p}_b}{(2\pi)^3 2p_{b0}} \dots \frac{g_i d^3 \mathbf{p}_i}{(2\pi)^3 2p_{i0}} \frac{g_j d^3 \mathbf{p}_j}{(2\pi)^3 2p_{j0}} \dots \\ &\times (2\pi)^4 \delta^{(4)}(p + p_a + p_b + \dots - p_i - p_j - \dots) \\ &\times |\mathcal{M}|_{i+j+\dots \rightarrow \Psi+a+b+\dots}^2 f_i f_j \dots \end{aligned}$$

(freeze-in)

Inflaton decay $\Phi \rightarrow \Psi + \Psi$

1. DM model



2. Reheating



3. Freeze-in



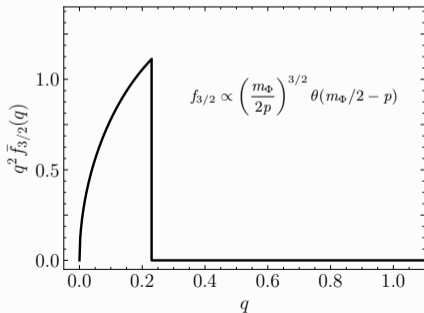
4. Constraints



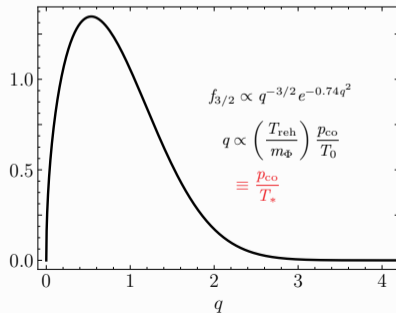
$$\frac{\partial f_{3/2}}{\partial t} - H|\mathbf{p}| \frac{\partial f_{3/2}}{\partial |\mathbf{p}|} \simeq \frac{1}{2p_0} \int \frac{g_{3/2} d^3 \mathbf{k}}{(2\pi)^3 2k_0} \frac{d^3 \mathbf{P}}{(2\pi)^3 2P_0} (2\pi)^4 \delta^{(4)}(P - p - k)$$

$$\times \frac{2\alpha_1^4 y_\nu^2 m_\Phi^2}{9\pi^4 M_P^4 m_{3/2}^4} \left[5 - 6 \ln \left(\frac{M_R^2}{m_\Phi^2} \right) \right]^2 (2\pi)^3 n_\Phi(t) \delta^{(3)}(\mathbf{P})$$

$t \ll t_{\text{reh}}$



$t \gg t_{\text{reh}}$



Inflaton decay $\Phi \rightarrow \Psi + \Psi$

1. DM model



2. Reheating



3. Freeze-in



4. Constraints



$$\frac{\partial f_{3/2}}{\partial t} - H|\mathbf{p}| \frac{\partial f_{3/2}}{\partial |\mathbf{p}|} \simeq \frac{1}{2p_0} \int \frac{g_{3/2} d^3 \mathbf{k}}{(2\pi)^3 2k_0} \frac{d^3 \mathbf{P}}{(2\pi)^3 2P_0} (2\pi)^4 \delta^{(4)}(P - p - k) \\ \times \frac{2\alpha_1^4 y_\nu^2 m_\Phi^2}{9\pi^4 M_P^4 m_{3/2}^4} \left[5 - 6 \ln \left(\frac{M_R^2}{m_\Phi^2} \right) \right]^2 (2\pi)^3 n_\Phi(t) \delta^{(3)}(\mathbf{P})$$

$$\Omega_{3/2} h^2 \simeq 0.1 \left(\frac{\alpha_1}{1.1 \times 10^{-8}} \right)^4 \left(\frac{m_\Phi}{3 \times 10^{13} \text{ GeV}} \right)^5 \left(\frac{0.15 \text{ eV}}{m_1} \right)^2 \\ \times \left(\frac{10^4 \text{ GeV}}{m_{3/2}} \right)^3 \left(\frac{T_{\text{reh}}}{10^{10} \text{ GeV}} \right) \times \frac{(\ln(M_R^2/m_\Phi^2) - 5/6)^2}{\ln^2(M_R^2/m_\Phi^2)}.$$

Light DM production from non-quadratic inflaton decay / preheating \rightarrow work in progress!

1. DM model



2. Reheating



3. Freeze-in

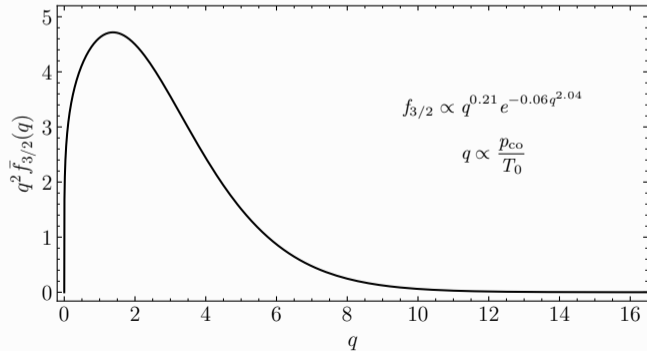


4. Constraints



Scatterings $H + \nu \rightarrow \Psi + B$

$$\frac{\partial f_{3/2}}{\partial t} - H|p| \frac{\partial f_{3/2}}{\partial |p|} \simeq \frac{1}{2p_0} \int \frac{2d^3\mathbf{p}'}{(2\pi)^3 2p'_0} \frac{d^3\mathbf{k}_1}{(2\pi)^3 2k_1^0} \frac{2d^3\mathbf{k}_2}{(2\pi)^3 2k_2^0} (2\pi)^4 \delta^{(4)}(p + p' - k_1 - k_2) \\ \times \left(-\frac{8}{3} \frac{\alpha_1^2 y^2}{m_{3/2}^2 M_R^2 M_P^2} s^2 t \right) \frac{1}{e^{k_1/T} + 1} \frac{1}{e^{k_2/T} - 1}$$



1. DM model



2. Reheating



3. Freeze-in



4. Constraints



Scatterings $H + \nu \rightarrow \Psi + B$

$$\frac{\partial f_{3/2}}{\partial t} - H|\mathbf{p}| \frac{\partial f_{3/2}}{\partial |\mathbf{p}|} \simeq \frac{1}{2p_0} \int \frac{2d^3\mathbf{p}'}{(2\pi)^3 2p'_0} \frac{d^3\mathbf{k}_1}{(2\pi)^3 2k_1^0} \frac{2d^3\mathbf{k}_2}{(2\pi)^3 2k_2^0} (2\pi)^4 \delta^{(4)}(p + p' - k_1 - k_2) \\ \times \left(-\frac{8}{3} \frac{\alpha_1^2 y^2}{m_{3/2}^2 M_R^2 M_P^2} s^2 t \right) \frac{1}{e^{k_1/T} + 1} \frac{1}{e^{k_2/T} - 1}$$

$$\Omega_{3/2} h^2 \simeq 0.1 \left(\frac{\alpha_1}{1.1 \times 10^{-3}} \right)^2 \left(\frac{427/4}{g_{\text{reh}}} \right)^{3/2} \left(\frac{T_{\text{reh}}}{10^{10} \text{ GeV}} \right)^5 \\ \times \left(\frac{m_1}{0.15 \text{ eV}} \right) \left(\frac{10^{14} \text{ GeV}}{M_R} \right) \left(\frac{10^4 \text{ GeV}}{m_{3/2}} \right)$$

(quadratic inflaton potential)

1. DM model



2. Reheating



3. Freeze-in



4. Constraints



Scatterings $H + \nu \rightarrow \Psi + B$

$$\frac{\partial f_{3/2}}{\partial t} - H|\mathbf{p}| \frac{\partial f_{3/2}}{\partial |\mathbf{p}|} \simeq \frac{1}{2p_0} \int \frac{2d^3\mathbf{p}'}{(2\pi)^3 2p'_0} \frac{d^3\mathbf{k}_1}{(2\pi)^3 2k_1^0} \frac{2d^3\mathbf{k}_2}{(2\pi)^3 2k_2^0} (2\pi)^4 \delta^{(4)}(p + p' - k_1 - k_2) \\ \times \left(-\frac{8}{3} \frac{\alpha_1^2 y^2}{m_{3/2}^2 M_R^2 M_P^2} s^2 t \right) \frac{1}{e^{k_1/T} + 1} \frac{1}{e^{k_2/T} - 1}$$

$$\Omega_{3/2} h^2 \simeq 0.1 \left(\frac{\alpha_1}{2 \times 10^{-3}} \right)^2 \left(\frac{427/4}{g_{\text{reh}}} \right)^{3/2} \left(\frac{T_{\text{reh}}}{10^{10} \text{ GeV}} \right)^5 \\ \times \left(\frac{m_1}{0.15 \text{ eV}} \right) \left(\frac{10^{14} \text{ GeV}}{M_R} \right) \left(\frac{10^4 \text{ GeV}}{m_{3/2}} \right) \left(\frac{T_{\text{max}}}{T_{\text{reh}}} \right)^{10/3}$$

(quartic inflaton potential, $\phi \rightarrow \bar{f}f$)

1. DM model



2. Reheating



3. Freeze-in

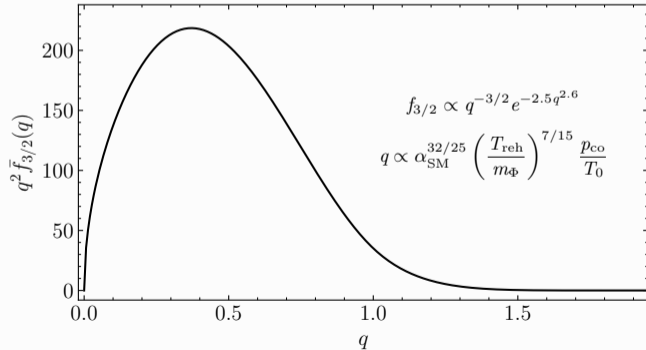


4. Constraints



Scatterings $H + \nu \rightarrow \Psi + B$

$$\frac{\partial f_{3/2}}{\partial t} - H|\mathbf{p}| \frac{\partial f_{3/2}}{\partial |\mathbf{p}|} \simeq \frac{1}{2p_0} \int \frac{2d^3\mathbf{p}'}{(2\pi)^3 2p'_0} \frac{d^3\mathbf{k}_1}{(2\pi)^3 2k_1^0} \frac{2d^3\mathbf{k}_2}{(2\pi)^3 2k_2^0} (2\pi)^4 \delta^{(4)}(p + p' - k_1 - k_2) \\ \times \left(-\frac{8}{3} \frac{\alpha_1^2 y^2}{m_{3/2}^2 M_R^2 M_P^2} s^2 t \right) \text{Br}_\nu \left(\frac{24\pi^2 \Gamma_\Phi t n_\Phi}{m_\Phi^3} \right)^2 \left(\frac{m_\Phi^2}{4k_1 k_2} \right)^{3/2} \theta\left(\frac{m_\Phi}{2} - k_1\right) \theta\left(\frac{m_\Phi}{2} - k_2\right)$$



1. DM model



2. Reheating



3. Freeze-in



4. Constraints



Scatterings $H + \nu \rightarrow \Psi + B$

$$\frac{\partial f_{3/2}}{\partial t} - H|p| \frac{\partial f_{3/2}}{\partial |p|} \simeq \frac{1}{2p_0} \int \frac{2d^3 p'}{(2\pi)^3 2p'_0} \frac{d^3 k_1}{(2\pi)^3 2k_1^0} \frac{2d^3 k_2}{(2\pi)^3 2k_2^0} (2\pi)^4 \delta^{(4)}(p + p' - k_1 - k_2) \\ \times \left(-\frac{8}{3} \frac{\alpha_1^2 y^2}{m_{3/2}^2 M_R^2 M_P^2} s^2 t \right) \text{Br}_\nu \left(\frac{24\pi^2 \Gamma_\Phi t n_\Phi}{m_\Phi^3} \right)^2 \left(\frac{m_\Phi^2}{4k_1 k_2} \right)^{3/2} \theta\left(\frac{m_\Phi}{2} - k_1\right) \theta\left(\frac{m_\Phi}{2} - k_2\right)$$

$$\Omega_{3/2} h^2 \simeq 0.1 \left(\frac{\alpha_1}{1.1 \times 10^{-3}} \right)^2 \left(\frac{0.030}{\alpha_{\text{SM}}} \right)^{16/5} \left(\frac{m_1}{0.15 \text{ eV}} \right) \left(\frac{g_{\text{reh}}}{427/4} \right)^{7/10} \left(\frac{10^4 \text{ GeV}}{m_{3/2}} \right) \\ \times \left(\frac{10^{14} \text{ GeV}}{M_R} \right) \left(\frac{m_\Phi}{3 \times 10^{13} \text{ GeV}} \right)^{14/5} \left(\frac{T_{\text{reh}}}{10^{10} \text{ GeV}} \right)^{19/5} \left(\frac{\mathcal{B}_1}{7 \times 10^{-4}} \right)$$

Thermalization in non-quadratic reheating to be determined

1. DM model



2. Reheating



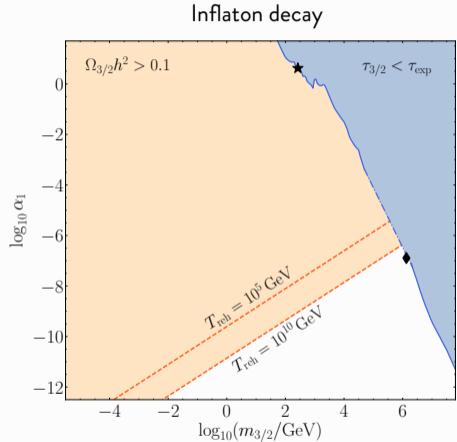
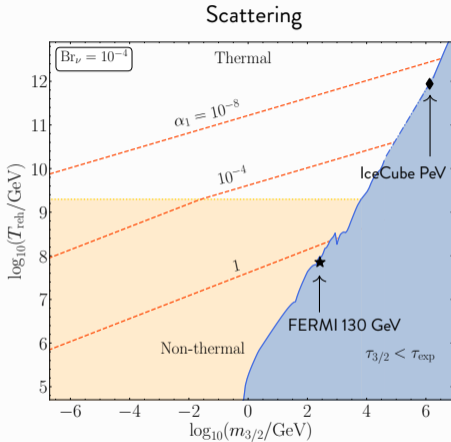
3. Freeze-in



4. Constraints



Constraints: $\Omega_{\text{DM}} + \gamma + \nu$



1. DM model



2. Reheating



3. Freeze-in

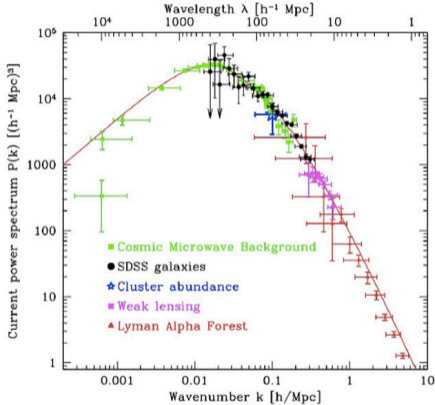


4. Constraints

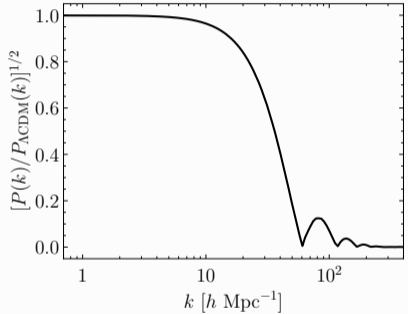


How warm is out-of-equilibrium dark matter?

Light DM \rightarrow free streaming \rightarrow suppression of structure



N. Palanque-Delabrouille et al., JCAP 04 (2020), 038
 A. Garzilli et al., 1912.09397 [astro-ph.CO]



Absence of cutoff for freeze-out relic

$$\Rightarrow m_{\text{WDM}} \gtrsim 3 \text{ keV}$$

1. DM model



2. Reheating



3. Freeze-in



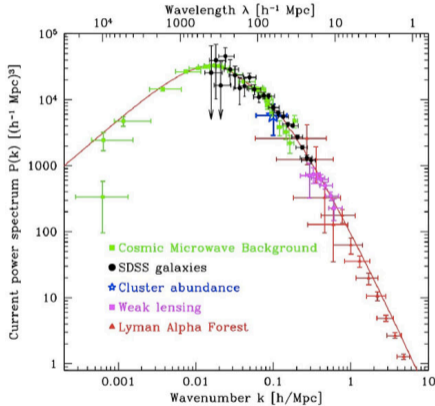
4. Constraints



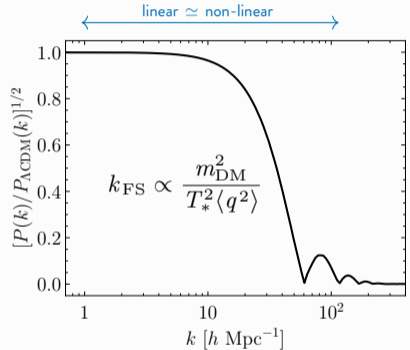
How warm is out-of-equilibrium dark matter?

For non-equilibrated DM,

R. Murgia, V. Iršič and M. Viel, PRD 98 (2018), 083540



G. Ballesteros, MG and M. Pierre, JCAP 03 (2021), 101



$$m_{\text{DM}} = m_{\text{WDM}} \left(\frac{T_*}{T_{\text{WDM}}} \right) \sqrt{\frac{\langle q^2 \rangle}{\langle q^2 \rangle_{\text{WDM}}}}$$

How warm is out-of-equilibrium dark matter?

DM from inflaton decay:

$$m_{3/2} > 3.8 \text{ MeV} \left(\frac{m_\Phi}{3 \times 10^{13} \text{ GeV}} \right) \left(\frac{10^{10} \text{ GeV}}{T_{\text{reh}}} \right)$$

Thermal freeze-in, (α_1):

$$m_{3/2} > 8.5 \text{ keV}$$

Non-thermal freeze-in, (α_1):

$$m_{3/2} > 0.4 \text{ keV} \left(\frac{\alpha_{\text{SM}}}{0.03} \right)^{-32/15} \left(\frac{m_\Phi}{3 \times 10^{13} \text{ GeV}} \right)^{23/15} \left(\frac{10^{10} \text{ GeV}}{T_{\text{reh}}} \right)^{7/15}$$

1. DM model



2. Reheating



3. Freeze-in



4. Constraints



1. DM model



2. Reheating



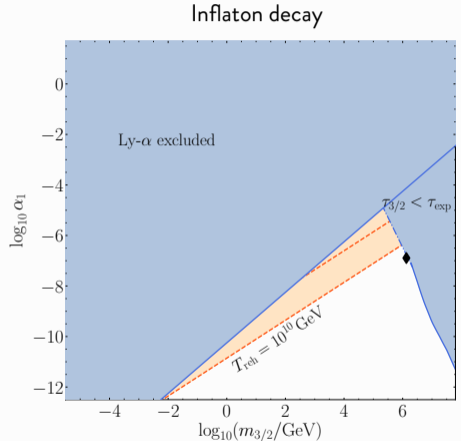
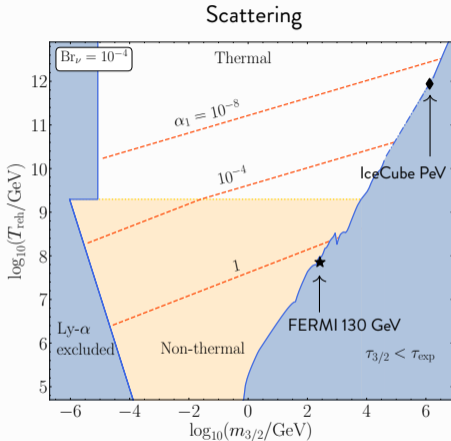
3. Freeze-in



4. Constraints



Constraints: $\Omega_{DM} + \gamma + \nu + \text{Lyman-}\alpha$



Thank you!